

Algebra 1: 6.1 (Part 1) HW
Solving Systems by Graphing

Name Answer Key Period _____

Write a system of linear equations to represent each scenario. Define each variable. Then, graph the system of equations. Use the graph to estimate the break-even point, then calculate the exact break-even point. Explain what the break-even point represents with respect to each scenario. Round to the 100th place.

1. Diamond sets up a lemonade stand in front of her house. Each cup of lemonade costs Diamond \$0.30 to make, and she spends \$6 on the advertising signs she puts up around the neighborhood. She sells each cup of lemonade for \$1.50.

$x = \#$ of cups of lemonade

Income equation:

$$y = 1.50x$$

Expense equation:

$$y = 0.3x + 6$$

Break-even Point estimate: (Pt of intersection)

$$x = 5 \text{ or } (5, 7.5)$$

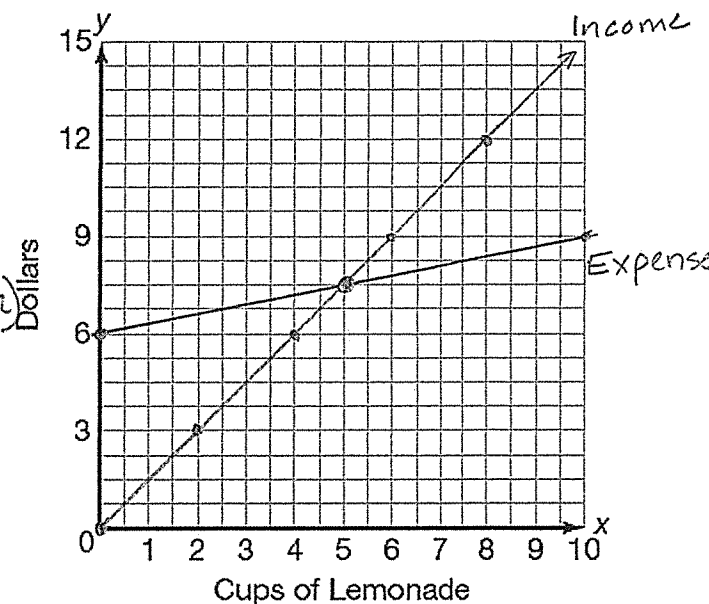
Break-even Point exact:

$$y = 1.50x \text{ and } y = 0.3x + 6$$

$$1.50x = 0.3x + 6$$

$$1.2x = 6$$

$$x = 5$$



What does the break-even point represent?

Diamond must sell 5 cups of lemonade to break-even. Her income and expenses will be \$7.50.

2. Tyler starts his own lawn mowing business. He spends \$180 on a new lawnmower. For each yard he mows, he receives \$20 and spends \$4 on gas.

$x = \#$ of yards he mows

Income equation:

$$y = 20x$$

Expense equation:

$$y = 4x + 180$$

Break-even Point estimate:

x is between 11 and 12

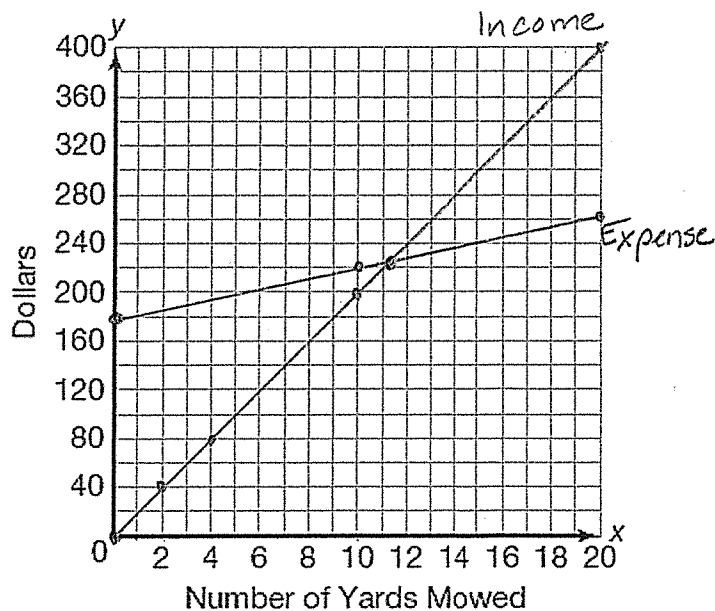
Break-even Point exact:

$$y = 20x \text{ and } y = 4x + 180$$

$$20x = 4x + 180$$

$$16x = 180$$

$$x = 11.25$$



What does the break-even point represent?

Tyler must mow between 11 and 12 yards to break-even. Her income and expenses will be \$225.

3. Mareshah is building birdhouses to raise money for a trip to Hawaii. She spends \$30 on the tools needed to build the houses. The material to build each birdhouse costs \$3.25. Olivia sells each birdhouse for \$10.

$x = \#$ of birdhouses

Income equation:

$$y = 10x$$

Expense equation:

$$y = 3.25x + 30$$

Break-even Point estimate:

x is between 4 and 5

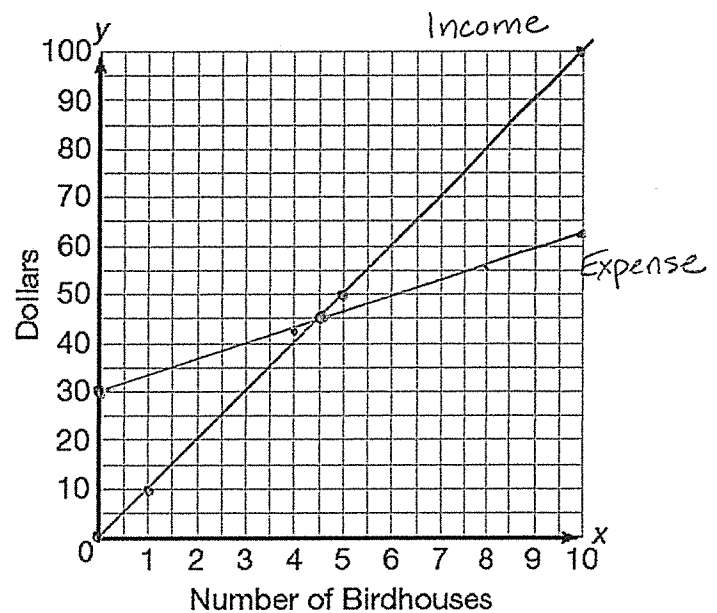
Break-even Point exact:

$$y = 10x \text{ and } y = 3.25x + 30$$

$$10x = 3.25x + 30$$

$$6.75x = 30$$

$$x = 4.44$$



What does the break-even point represent?

Mareshah must build between 4 and 5 birdhouses to break-even. Her income and expenses will be \$44.44

4. The Spanish Club is selling boxes of fruit as a fundraiser. The fruit company charges the Spanish Club \$7.50 for each box of fruit and a shipping and handling fee of \$100 for the entire order. The Spanish Club sells each box of fruit for \$15.

$x = \#$ of boxes of fruit

Income equation:

$$y = 15x$$

Expense equation:

$$y = 7.5x + 100$$

Break-even Point estimate:

x is between 13 and 14

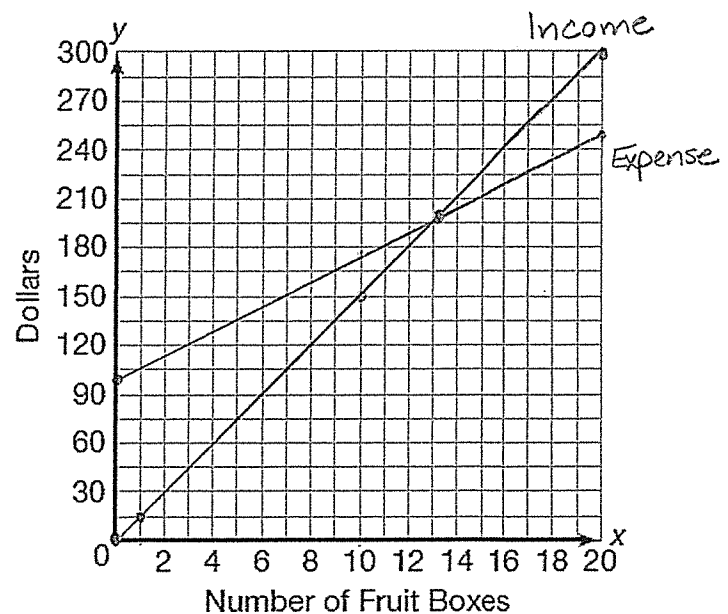
Break-even Point exact:

$$y = 15x \text{ and } y = 7.5x + 100$$

$$15x = 7.5x + 100$$

$$7.5x = 100$$

$$x = 13.33$$



What does the break-even point represent?

The Spanish Club must sell between 13 and 14 boxes of fruit to break-even. Their income and expenses will be \$200.